



ARRAYCON - ESR1

# Smart structures modelling and model order reduction techniques for feasible distributed active damping solutions

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# Future activities and difficulties

## PAPER SUMMARY:

### 1. Introduction

Citing references and the description for the use of this method

### 2. Neutral surface location for a wafer bonded to a plate

The arguments of the method to find the new neutral surface in the section of the structure, relation with the existed method

### 3. Smart materials' strain variation analysis

Focus on the bending moment, to show how to estimate the curvature and the strain

### 4. Results comparison and discussion

some FEM simulation results compare with the analytical results

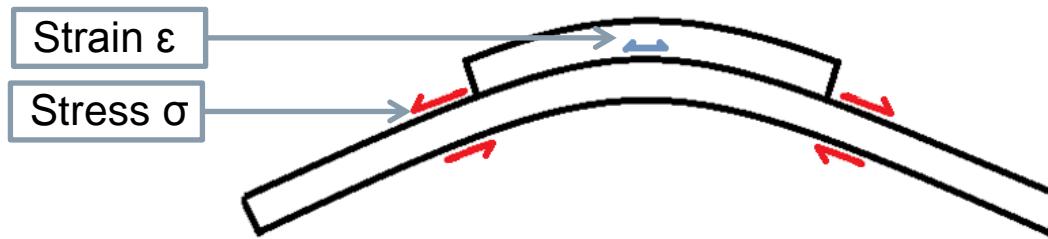
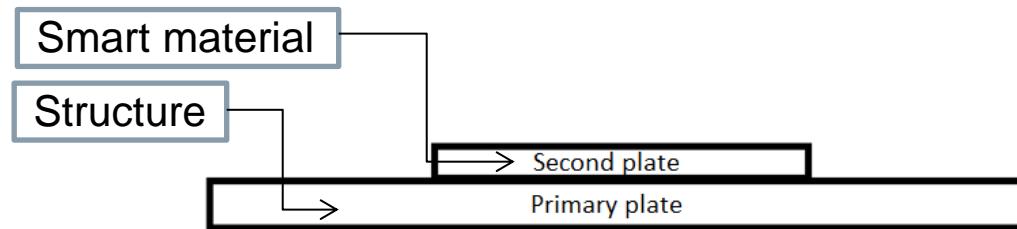
comparison between the analytical results with the references results

### 5. Conclusion

# Recent work

**DONE:**

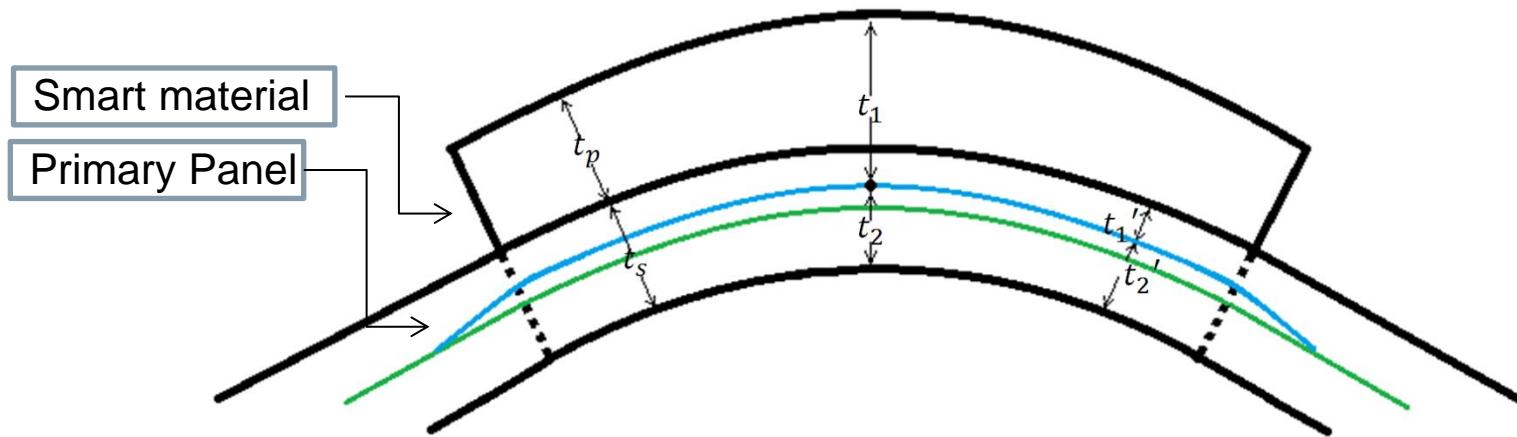
1. Mechanical coupling analysis between primary panel and smart material
2. Mechanical coupling simulations



# Recent work

## MECHANICAL ANALYSIS:

Kirchhoff's plate hypothesizes satisfied!!!



- a) Existence of the neutral axis in the primary panel
- b) Retention of the neutral axis in the primary panel section
- c) Smart material in tension and bending
- d) Exaltation of the neutral axis' location

# Recent work

## MECHANICAL ANALYSIS:

Determinate the neutral axis location

**The normal efforts on the neutral axis = null**

$$N_x = -\frac{E^+ t_1'^2}{2(1-(\vartheta^+)^2)} \left( \frac{\partial^2 w}{\partial x^2} + \vartheta^+ \frac{\partial^2 w}{\partial y^2} \right) - \frac{E_p [(t_1' + t_p)^2 - t_1'^2]}{2(1-(\vartheta_p)^2)} \left( \frac{\partial^2 w}{\partial x^2} + v_p \frac{\partial^2 w}{\partial y^2} \right) + \frac{E^- t_2^2}{2(1-(\vartheta^-)^2)} \left( \frac{\partial^2 w}{\partial x^2} + \vartheta^- \frac{\partial^2 w}{\partial y^2} \right) = 0$$

$$N_y = -\frac{E^+ t_1'^2}{2(1-(\vartheta^+)^2)} \left( \frac{\partial^2 w}{\partial y^2} + \vartheta^+ \frac{\partial^2 w}{\partial x^2} \right) - \frac{E_p [(t_1' + t_p)^2 - t_1'^2]}{2(1-(\vartheta_p)^2)} \left( \frac{\partial^2 w}{\partial y^2} + v_p \frac{\partial^2 w}{\partial x^2} \right) + \frac{E^- t_2^2}{2(1-(\vartheta^-)^2)} \left( \frac{\partial^2 w}{\partial y^2} + \vartheta^- \frac{\partial^2 w}{\partial x^2} \right) = 0$$

After the simplification

$$\frac{E_s(t_2^2 - t_1'^2)}{2(1-v_s)} = \frac{E_p [(t_1' + t_p)^2 - t_p^2]}{2(1-v_p)}$$

with  $t = t_p + t_s = t_1 + t_2$  &  $t_s = t_1' + t_2$

Finally

$$t_1' = \frac{\alpha t_s^2 - \beta t_p^2}{2(\beta t_p + \alpha t_s)}, \text{ which, } \alpha = \frac{1-v_p}{1-v_s} \text{ & } \beta = \frac{E_p}{E_s}$$

So

$$t_1 = t_p + t_1' \text{ & } t_2 = t - t_1$$

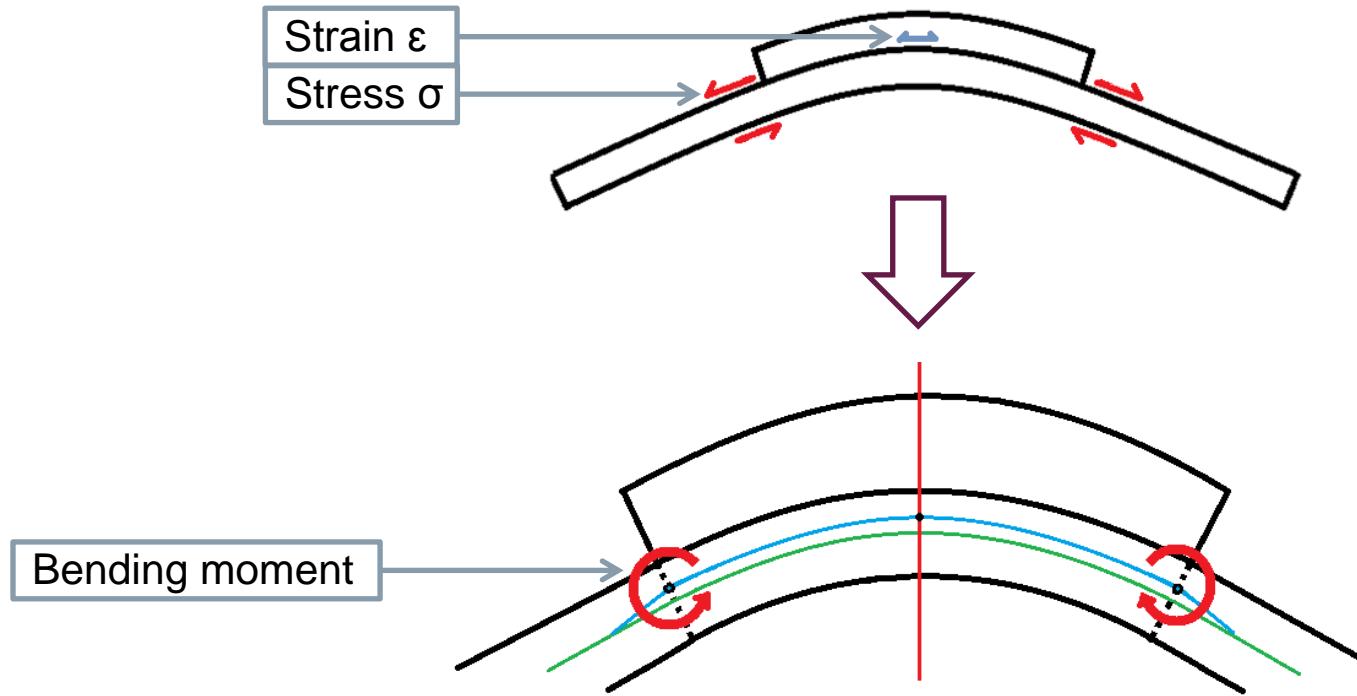
Test case:  $\alpha = \beta = 1$  (Isotropic homogenous materials ):  $t_1 = t_2 = \frac{t}{2}$

# Recent work

## MECHANICAL ANALYSIS:

Determinate the strain in the smart material

**Conservation of the moments in x and y directions**



# Recent work

## MECHANICAL ANALYSIS:

$$M_x: -a \frac{E^+ t_1^3}{3(1-(\vartheta^+)^2)} (\theta_x + \vartheta^+ \theta_y) - a \frac{E^- t_2^3}{3(1-(\vartheta^-)^2)} (\theta_x + \vartheta^- \theta_y) - a' \frac{E_p [(t_1' + t_p)^3 - t_1'^3]}{3(1-(v_p)^2)} (\theta_x + v_p \theta_y) = -a \frac{E_s t^3}{12(1-\nu^2)} (\theta_x^s + \vartheta \theta_y^s)$$

$$M_y: -b \frac{E^+ t_1^3}{3(1-(\vartheta^+)^2)} (\theta_y + \vartheta^+ \theta_x) - b \frac{E^- t_2^3}{3(1-(\vartheta^-)^2)} (\theta_y + \vartheta^- \theta_x) - b' \frac{E_p [(t_1' + t_p)^3 - t_1'^3]}{3(1-(v_p)^2)} (\theta_y + v_p \theta_x) = -b \frac{E_s t^3}{12(1-\nu^2)} (\theta_y^s + \vartheta \theta_x^s)$$

$\theta_x = \frac{\partial^2 w}{\partial x^2}$  &  $\theta_y = \frac{\partial^2 w}{\partial y^2}$  : curvature of the neutral layer in x & y directions

With

$$\varepsilon_{xx} = -z \frac{\partial^2 w}{\partial x^2} = -z \theta_x$$

$$\varepsilon_{yy} = -z \frac{\partial^2 w}{\partial y^2} = -z \theta_y$$

Finally,

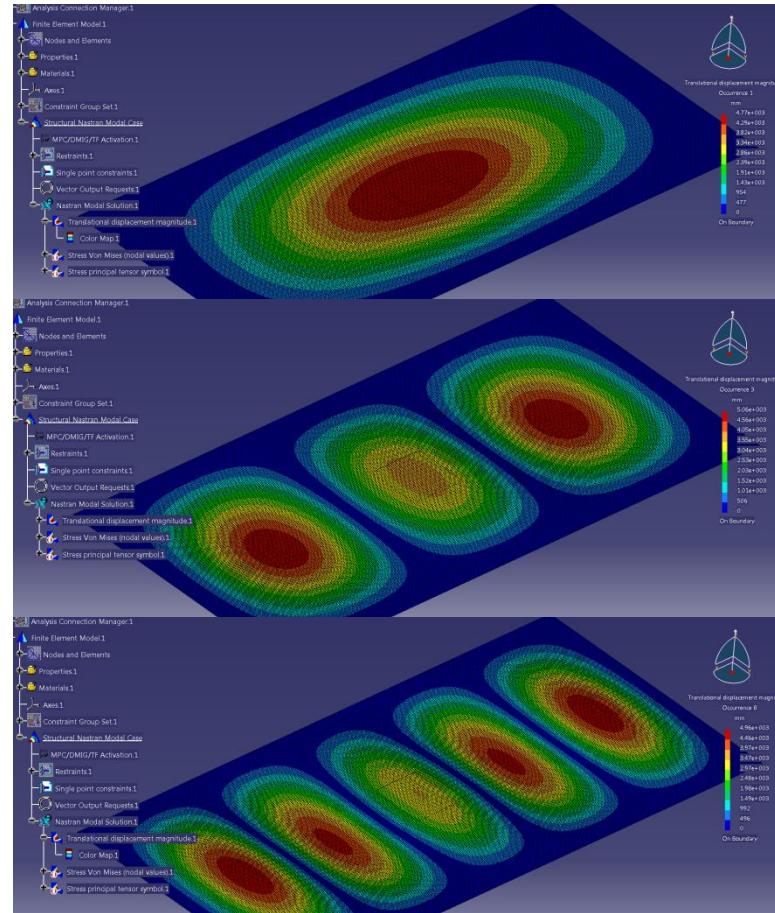
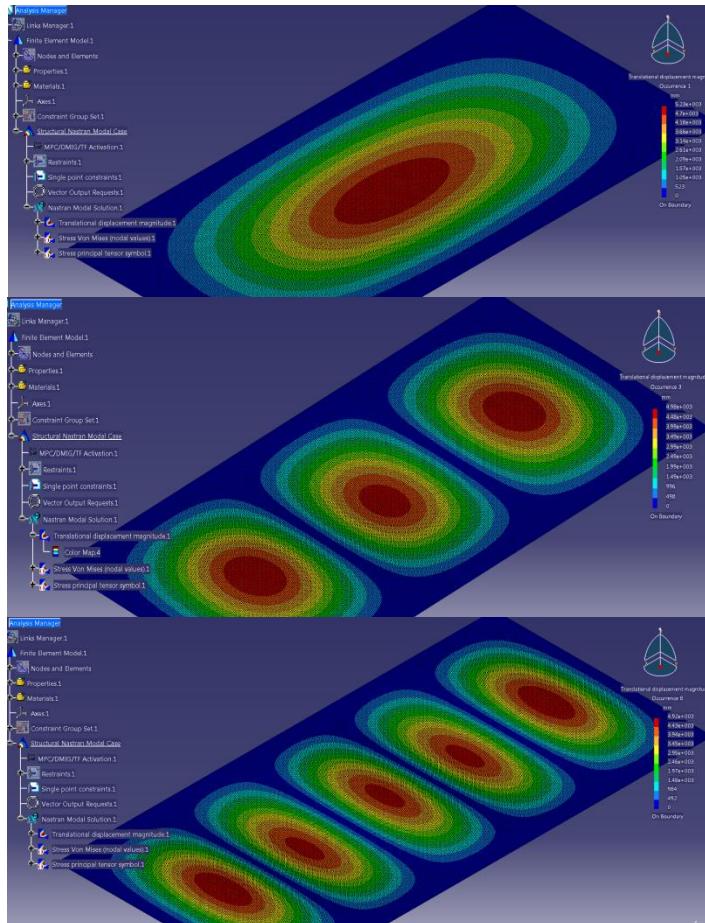
$$\varepsilon_{xx} = \frac{2z}{t_s} \left[ \frac{[(aD\gamma_1 - bD\gamma_3 v_s) \varepsilon_{xx}^s + (aD\gamma_2 v_s - bD\gamma_3) \varepsilon_{yy}^s]}{(\gamma_1\gamma_2 - \gamma_3\gamma_4)} \right]$$

$$\varepsilon_{yy} = \frac{2z}{t_s} \left[ \frac{[(aD\gamma_2 - bD\gamma_1 v_s) \varepsilon_{xx}^s + (aD\gamma_4 v_s - bD\gamma_1) \varepsilon_{yy}^s]}{(\gamma_3\gamma_4 - \gamma_1\gamma_2)} \right]$$

$\gamma_1, \gamma_2, \gamma_3, \gamma_4$ : factors from the Moments equations

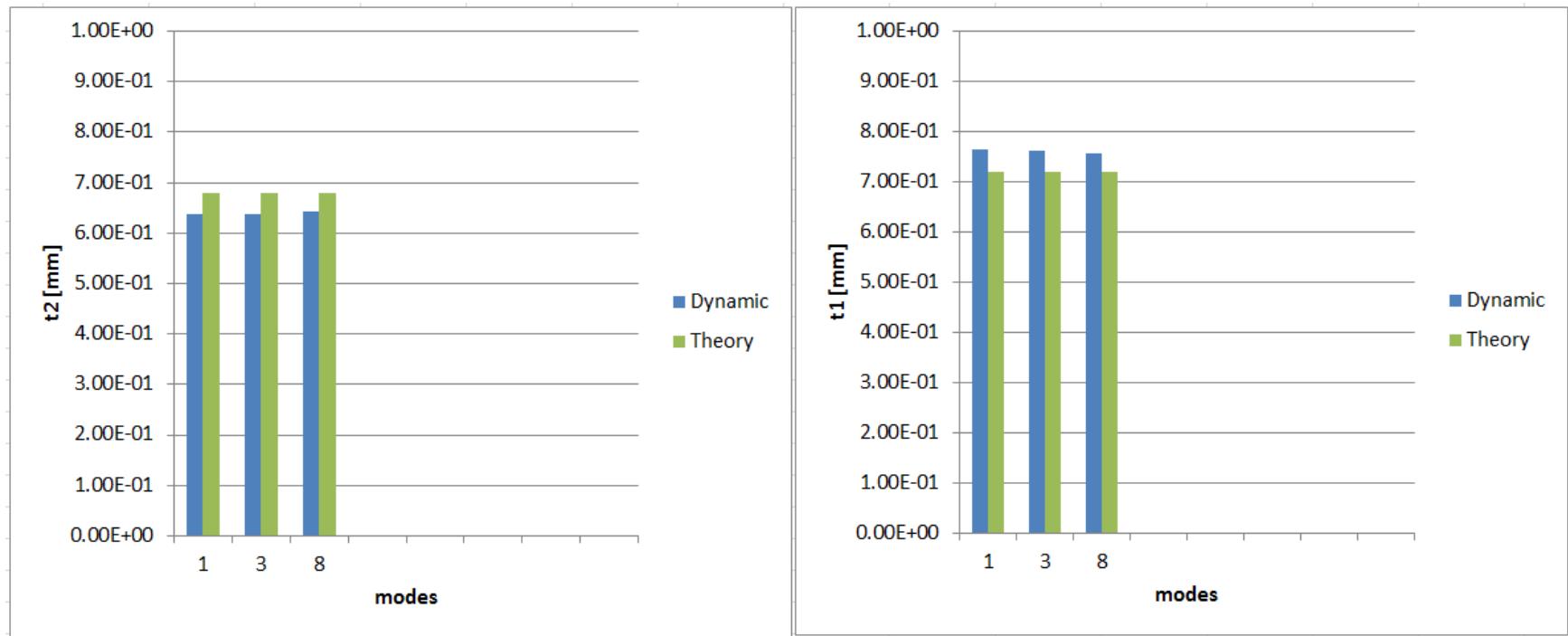
## Recent work

# ONE SMART MATERIAL NUMERICAL SIMULATIONS:



# Recent work

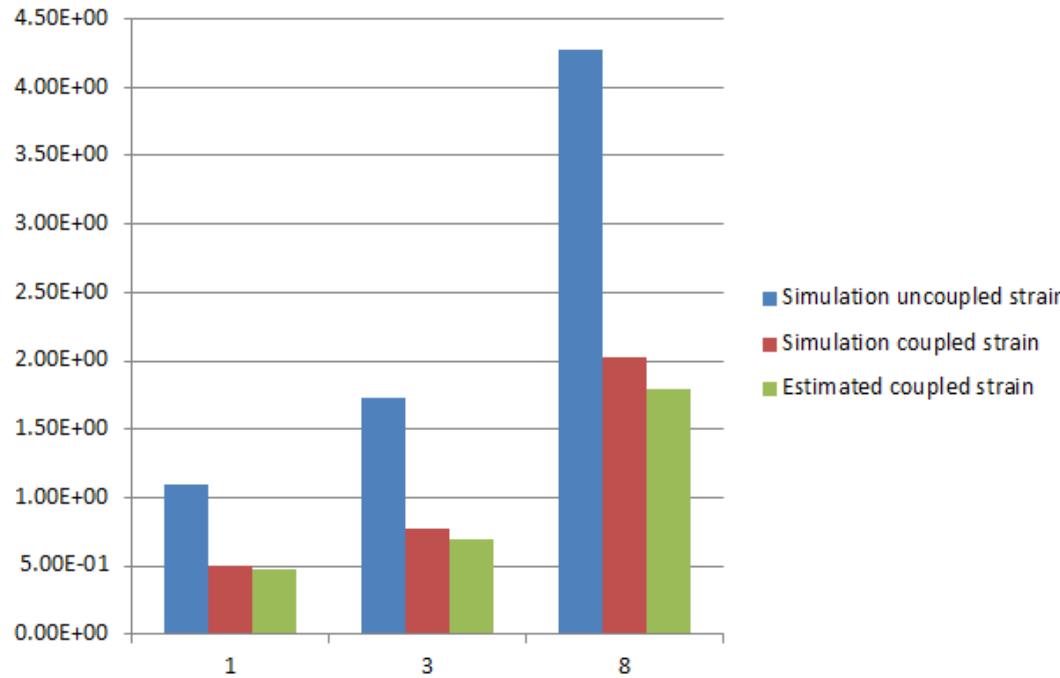
## ONE SMART MATERIAL NUMERICAL SIMULATIONS :



Neutral axis position: Error between analytical solution and simulation: 5%

# Recent work

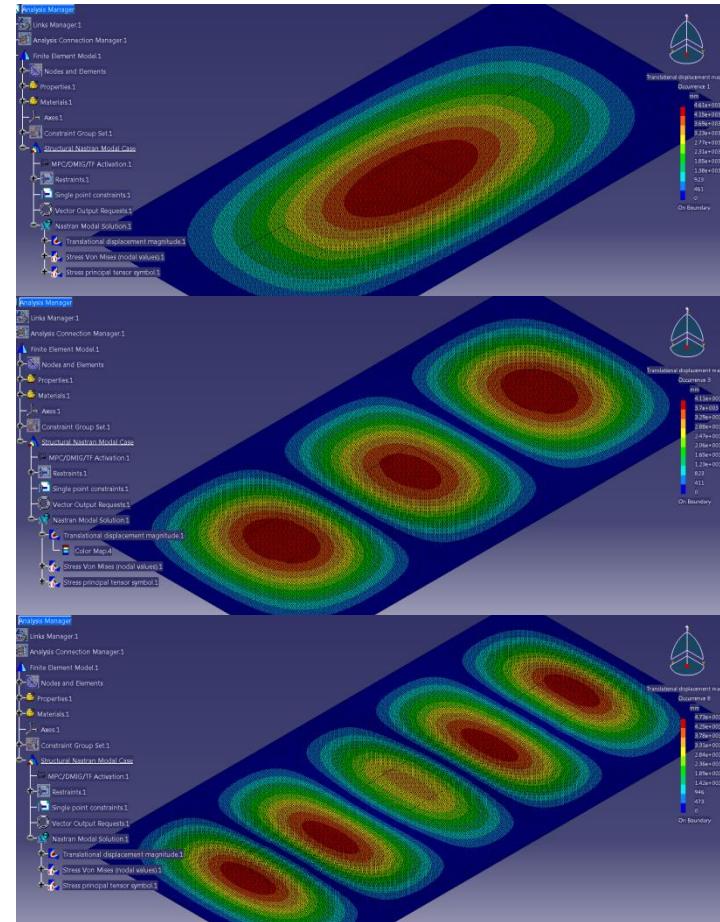
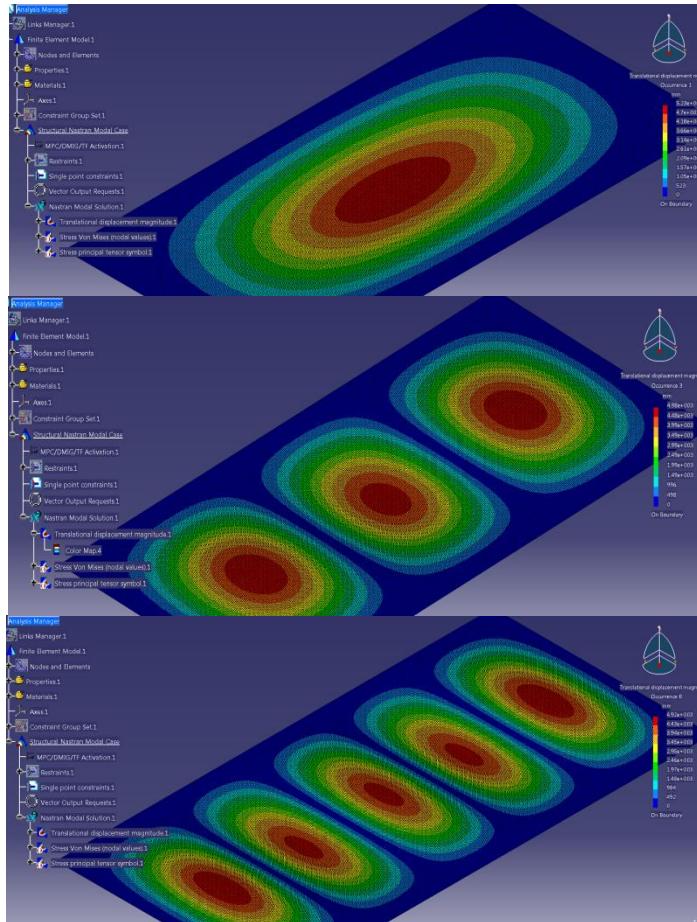
## ONE SMART MATERIAL NUMERICAL SIMULATIONS :



mode	Simulation uncoupled strain	Simulation coupled strain	Estimated coupled strain	relative error
1	1.10E+00	5.08E-01	4.72E-01	6%
3	1.73E+00	7.76E-01	6.97E-01	8%
8	4.27E+00	2.03E+00	1.80E+00	10%

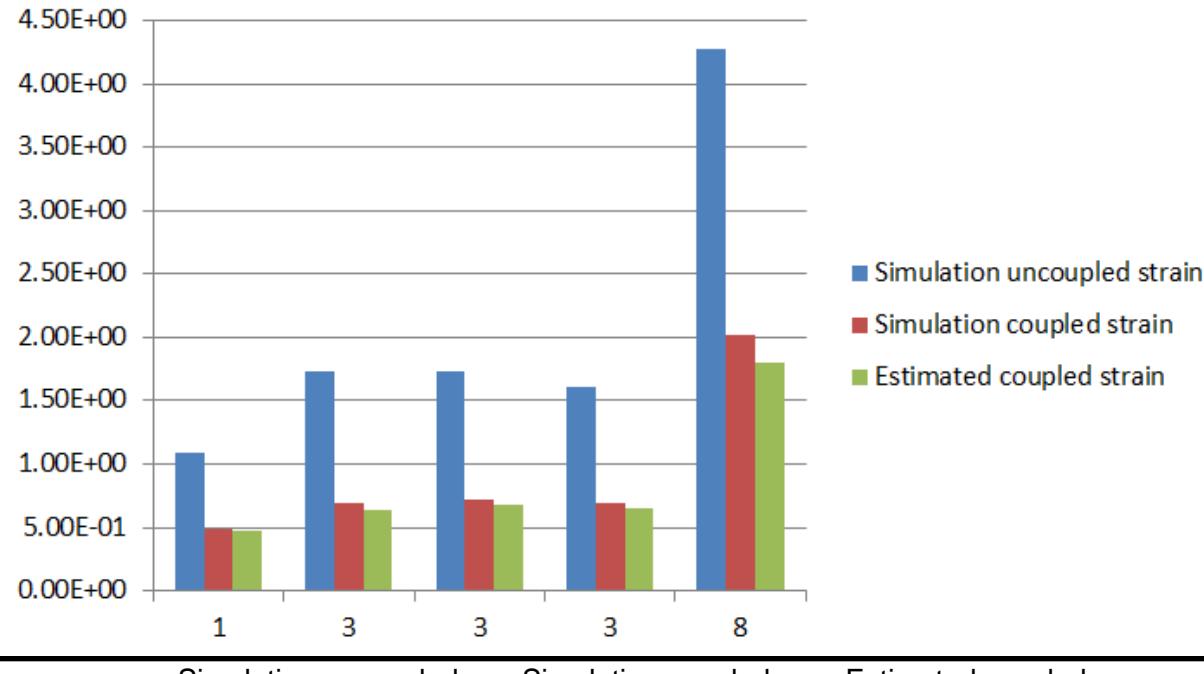
# Recent work

# THREE SMART MATERIAL NUMERICAL SIMULATIONS :



# Recent work

## THREE SMART MATERIAL NUMERICAL SIMULATIONS :



mode	Simulation uncoupled strain	Simulation coupled strain	Estimated coupled strain	relative error
1	1.10E+00	4.93E-01	4.72E-01	3%
3	1.73E+00	6.90E-01	6.35E-01	5%
3	1.73E+00	7.21E-01	6.82E-01	4%
3	1.61E+00	6.90E-01	6.56E-01	4%
8	4.27E+00	2.02E+00	1.80E+00	10%

# Future activities and difficulties

## WORK TO ACHIEVE:

1. Piezoelectric-mechanic relation of smart materials (literature search)
2. More detail FEM simulations
3. Results comparison with the literature references